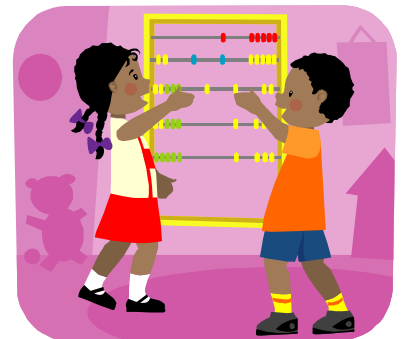




St. Peter's Catholic Primary School

# Helping your child with written calculations in Maths





## Introduction

This booklet is designed to illustrate the variety of approaches to solving number problems that your child will be taught at our school.

## Why Write It?

Calculations may be recorded:

- to make informal jottings of the steps on the way to an answer
- to develop the skill of explaining the method used
- to help someone else follow that method, perhaps to assess their work
- to practise writing and using correct symbols and notation (e.g. + - x ÷)
- to help remember or to practise the recall of number facts (e.g.  $7+3=10$   $70+30=100$ )
- to carry out the working of a standard written method of calculation

## ADDITION

### Skills in Early Addition

- Counting all – a child doing  $2 + 3$  counts out two bricks and then three bricks and then finds the total by counting all the bricks.
- Counting on from the first number – a child finding  $3 + 5$  counts on from the first number; 'four, five, six, seven, eight'.
- Counting on from the larger number – a child chooses the larger number, even when it is not the first number and counts on from there.

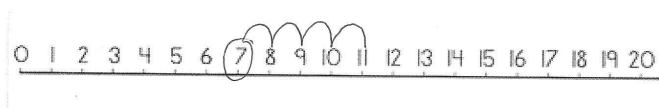
### Mental Skills in Addition

- Using a known addition fact – where a child gives an immediate response to facts known by heart, such as  $6+4$  or  $3+3$  or  $10+8$ .
- Using a known fact to derive a new fact – where a child uses a number bond that they know by heart to calculate one that she or he does not know, e.g. using knowledge that  $5+5=10$  to work out  $5+6=11$  and  $5+7=12$ .
- Using knowledge of place value – where a child uses knowledge that  $4+3=7$  to work out  $40+30=70$ , or knowledge that  $46+10=56$  to work out  $46+11=57$ .

## Stages in Addition

1. Using a Number Line or 100 Square to count on in ones.

$$7 + 4 = 11$$



$$16 + 9 = 25$$

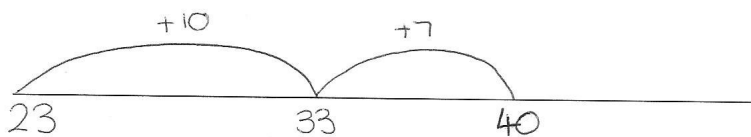
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

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2. Using Empty Number Lines

$$23 + 17 =$$

$$23 + 10 + 7 =$$



3. Vertical layout – expanded working, moving to adding the least significant digit first and extending to three digit numbers. Partial sums are added mentally.

$$\begin{array}{r}
 47 \\
 + 76 \\
 \hline
 13 \\
 110 \\
 \hline
 123
 \end{array}
 \quad
 \begin{array}{l}
 = 7 + 6 \\
 = 70 + 40
 \end{array}$$

$$\begin{array}{r}
 368 \\
 + 493 \\
 \hline
 11 \\
 150 \\
 700 \\
 \hline
 861
 \end{array}
 \quad
 \begin{array}{l}
 = 8 + 3 \\
 = 60 + 90 \\
 = 300 + 400
 \end{array}$$

4. Vertical layout, contracting the working to a compact, efficient form:

$$\begin{array}{r}
 \text{T U} \\
 47 \\
 + 76 \\
 \hline
 123 \\
 1 \quad 1
 \end{array}
 \quad
 \begin{array}{r}
 \text{H T U} \\
 368 \\
 + 493 \\
 \hline
 861 \\
 1 \quad 1
 \end{array}$$

#### Language used in compact methods

$$\begin{array}{r}
 547 \\
 + 276 \\
 \hline
 823 \\
 1 \quad 1
 \end{array}$$

- Seven plus six equals thirteen, write down three and carry ten (child writes carry digit underneath)
- Forty plus seventy equals one hundred and ten, plus the extra ten, which equals one hundred and twenty. Write down twenty and carry one hundred (child writes carry digit underneath)
- Five hundred plus two hundred equals seven hundred, plus the extra one hundred, which equals eight hundred.
- The total is eight hundred and twenty-three.

## SUBTRACTION

### Skills in Early Subtraction

- Counting out – a child finding  $9 - 3$  holds up nine fingers and folds down three.
- Counting back from – a child finding  $9 - 3$  counts back three numbers from 9; 'eight, seven, six'.
- Counting back to – a child doing  $11 - 7$  counts back from the first number to the second, keeping a tally using fingers of the number of numbers that have been said, 'ten, nine, eight, seven', holding up four fingers.
- Counting up – a child doing  $11 - 7$  counts up from 7 to 11, 'eight, nine, ten, eleven', sometimes keeping a count of the spoken numbers using fingers (not a 'natural' strategy for many children because of the widely held perception of subtraction as 'taking away').

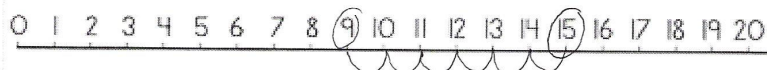
### Mental Skills in Subtraction

- Using a known fact – a child gives a rapid response based on facts known by heart, such as  $8 - 3$  or  $20 - 8$ .
- Using a derived fact – a child uses a known fact to work out a new one, e.g.  $20 - 5$  is 15, so  $20 - 6$  must be 14 (more unusual in subtraction than in addition).
- Using knowledge of place value – a child finding  $25 - 9$  knows that  $25 - 10$  is 15, and uses this to give an answer of 16.

## Stages in Subtraction

1. Using a Number Line or 100 Square to count back in ones.

$$15 - 6 = 9$$



$$15 - 13 = 2$$

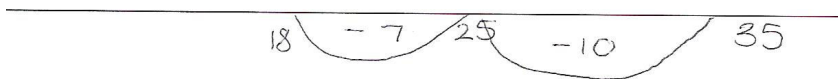
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

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2. Using Empty Number Lines

$$35 - 17 =$$

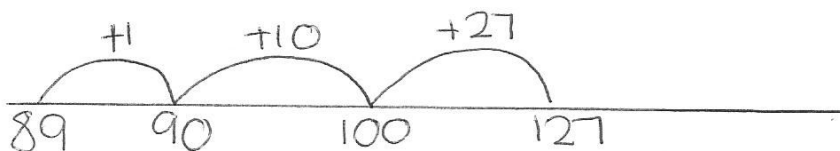
$$35 - 10 - 7 =$$





### 3. Finding the Difference on a Number Line

$$127 - 89$$



### 4. Finding the Difference by Counting On

$$\begin{array}{r} 127 \\ - 89 \\ \hline 10 + (90) \\ 10 + (100) \\ 27 + (127) \\ \hline 38 \end{array}$$

### 5. Subtraction Using the Compact Method

$$\begin{array}{r} 04 \ 112 \ 17 \\ 8 \ 9 \ - \\ \hline 3 \ 8 \end{array}$$

# MULTIPLICATION

## Mental Skills in Multiplication

- Starting with tables for 2 and 10, knowing by heart facts such as 'seven twos' or 'four tens', progressing to facts in the 5 times-table, then others.
- Recognising that multiplication can be done in any order – e.g. realising that  $5 \times 2$  is the same as  $2 \times 5$ .
- Doubling two digit numbers – double 10, 20, 30, 40 .... then, for example, double 23 as double 20 plus double 3.
- Using doubling e.g. working out the 4 times-table by doubling the 2 times-table.
- Using related facts – e.g.  $5 \times 4 = 20$  to find  $6 \times 4 = 24$ .
- Knowing by heart the 3 and 4 times-table.
- Recognising the effect of multiplying a number by 10.
- Approximating, e.g. working out  $19 \times 17$  by doing  $20 \times 17$  and then subtracting 17.

## Stages in Multiplication

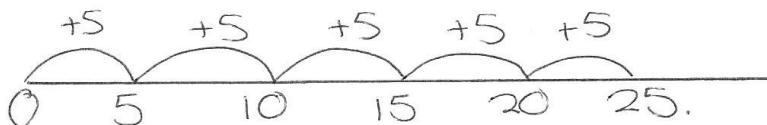
### 1. Working out 'groups of' 2, 5 and 10

$$5 \times 2 = 10$$



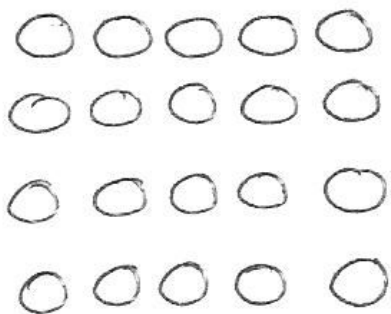
### 2. Repeated Addition on a Number Line

$$5 \times 5 = 25$$



### 3. Using Arrays

$$5 \times 4 = 20$$



### 4. The Grid Method

$$12 \times 5 =$$

5	10	2
	50	10

$$= 50 + 10 = 60$$

$$12 \times 12 =$$

10	2
10	100 20
2	20 4

$$= 100 + 20 + 20 + 4$$

$$= 144$$

### 5. The Column Method (1)

$$123 \times 6 =$$

1	2	3	
		6	X
	1	8	(u)
1	2	0	(T)
6	0	0	(H)
7	3	8	

### 6. The Column Method (2)

$$123 \times 6 =$$

1	2	3	
		6	X
7	3	8	
<sub>1</sub>	<sub>1</sub>		

### 7. The Column Method (3)

$$123 \times 24 =$$

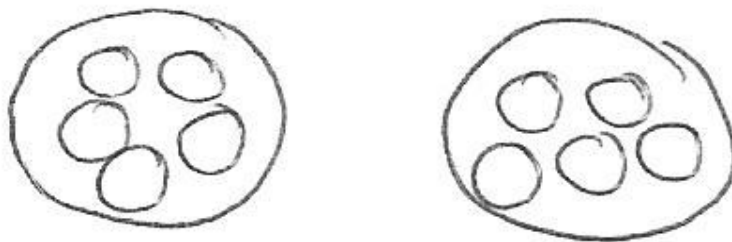
	1	2	3	
		2	4	X
	4	9	2	
2	4	6	0	

$123 \times 4$   
 $123 \times 20$

# DIVISION

## 1. Sharing

$$10 \div 2 = 5$$

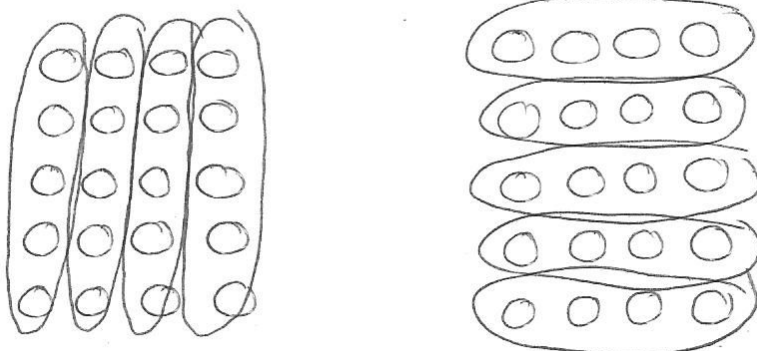


## 2. Grouping

$$10 \div 2 = 5$$

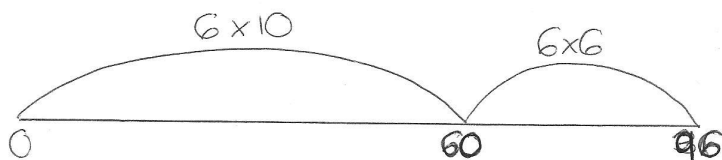


## 3. Using Arrays (starting with 2's, 5's, 10's and then move onto 3's and 4's)



## 4. Using a Number Line

$$96 \div 6 = 16$$



### 5. Short Division (1)

$$96 \div 6 =$$

$$\begin{array}{r} 6 \overline{) 96} \\ \underline{60} \quad 10 \times 6 \\ 36 \\ \underline{36} \quad 6 \times 6 \\ 0 \end{array}$$

### 6. Short Division (2)

$$6 \overline{) 16} \quad \begin{array}{l} 16 \\ \underline{36} \end{array}$$

### 7. Long Division

$$742 \div 25$$

$$\begin{array}{r} 25 \overline{) 742} \\ \underline{250} \quad \times 10 \\ 492 \\ \underline{250} \quad \times 10 \\ 242 \\ \underline{125} \quad \times 5 \\ 117 \\ \underline{100} \quad \times 4 \\ 17 \end{array}$$

$$= 29 \text{ r. } 17$$